

# **An Infinite Circle is a Straight Line**

For solo piano

**Ian Percy**

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... a thousand sounds of Pi ...

For solo piano

Analysis Score: Cycles 1 – 7

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2012/20

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... a thousand sounds of pi ...

The majority of this multiple movement work for solo piano was composed systematically from the first 1,000 decimal digits of Pi during the summer of 2012. Using a combination of Arnold Schoenberg's dodecaphonic technique and Arvo Pärt's extended tone rows, the piece started life as an analytical exercise, a theoretical study into the musical possibilities of composing with the linear properties of eternal numbers.

This is an analysis score documenting the process for all seven of the original cycles.

Pi is an eternal number; it is infinite and linear but is part of the equation used to calculate the circumference of a circle; a cyclic and self-contained shape. The composer was attracted by this contradiction and was intrigued by the realisation that if Pi is an 'infinite decimal', it could also be argued that the precise circumference of a circle is an unobtainable pursuit (an infinite elusive). Whilst researching the fundamentals of Pi, one stumbled across an area of research (or mode of thinking) referred to as 'philosophical mathematics', which, until then, one would have considered to be an oxymoron. A quotation accredited (with some dispute) to Johannes Kepler (1571-1630) stating that 'an infinite circle is a straight line' offered just 'a splash' of external narrative (and a title for the piece). Others have mused how, therefore, the maximum triangle must also be a straight line ...

### **The Rules of the Game:**

1. The cycles are a systematic setting of the first one thousand decimal digits of Pi.
2. Numbers are translated to musical pitch via Schoenberg's 12-tone system. C was chosen as 0, but the system is transposable.
3. Whenever 1, 0 or 1, 1 appear in the sequence, they are treated as 10 and 11. Without this anomaly (referred to as the 10/11 anomaly), Cycle One would outline a decachord (10-tone language) instead of the total chromatic (12-tone language).
4. Instead of returning to 0 at the octave (as in Schoenberg's method), the system was extended at each cycle (e.g. 0 = C2, 12 = C3 and 24 = C4 etc.), which expanded the registral span at each iteration and introduced an architectural sense of textural and timbral development.
5. Cycle One uses 0 – 11 (one chromatic octave), Cycle Two uses 0 – 23 (two chromatic octaves) and Cycle Three uses 0 – 35 etc.
6. Every single digit (1 – 9) is equal to the duration of a semi-quaver.
7. Every double digit (10 – 83) is equal to a quaver (two semi-quavers).
8. There are many repeated digits in the infinite decimal of Pi, which led to a lot of semi-quaver reiterations, so repeated numbers are given the durational value of the combined digits: 8, 8, 8 equals a dotted-quaver (three semi-quavers) and 9, 9, 9, 9 equals a crotchet (four semi-quavers).

### **Simply Systematic:**

One recalls exploring a variety of initial approaches whilst trying to uncover fragments of music within this linear eternal and the processes were excessively time consuming to document in score form, but once the 'rules of the game' were established, it was literally a case of 'inputting the data' and sitting back to let the systems and cycles unfold, entertained by the musicality one had discovered. The articulation and dynamics added during final realisation of the performance score simply enhanced the phrases that were already present; like applying oil to wood to emphasise the grain and preserve its natural beauty. One could pose the question: Whose music is this? Perhaps it belongs to the Akashic Record? Perhaps it is mine?

### **Variable Form:**

This is a virtuosic piece. Cycle Seven borders on a 'mission impossible' and is perhaps more practical for performance as a duo for two players at one piano. Cycle Six demands elite acrobatics from the pianist and Cycle Five requires a high level of stamina, technique and agility. The music clearly belongs to the same evolutionary strand as George Antheil's *Ballet Mécanique* (1924) and Conlon Nancarrow's mid-twentieth-century studies for automated player pianos, and this collection was initially conceived as a theoretical exercise (not for the concert hall), but it is difficult to deny the inherent musicality in these cycles (and the capabilities of the modern pianist), so ...

**Notation:** This is an extremely chromatic score, so in order to dilute the number of accidentals, the following rules were strictly observed:

- a. The barline cancels all accidentals.
- b. Both staves are considered separate, so no cautionary naturals are offered.
- c. Accidentals (and their cautionaries) only apply to notes in that specific register.
- d. Whenever there are cross-staff beamed notes, no rests are given in either stave.

### **In Conclusion:**

The Cycles were composed through systematic translation of the first one thousand decimal digits of Pi into musical pitch, and, when using these rules, sounds like a form of contemporary chromatic Jazz. One is left wondering how the next 1,000 digits would sound if new rules were conceived in the context of a plainchant setting for SATB, or perhaps a modernist work for pitched percussion ...

# An Infinite Circle is a Straight Line

Note: Whenever 1, 0 or 1, 1 appear in the cycle, they are treated as 10 (B♭) and 11 (B♯) ...

Note: The barline cancels all accidentals.

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... a thousand sounds of pi ...

## Cycles 1 - 7

[Analysis score]

### Cycle 1 (a first of seven): The total chromatic ...

A ♩ = 104 Cycle 1: One octave span (0 - 11) C4 - B4 [transposable to any pitch at any register]: No reiterations (suspensions marked with an asterisk) ...

poco accel.

1 4 1 5 9 2 6 5 3 5 8 9 7 9 3 2 3 8 4 6 2 6 4 3\* 8 3 2 7 9 5 0 2 8\* 4 1 9 7 1 6 9 3 9\* 3 7 5 10 5 8 2 0 9 7 4 9 4\* 5 9 2 3 0 7 8 1 6 4 0 6 2 8 6 2 0 8 9\* 8 6 2 8 0 3 4 8 2 5 3 4 2 11 7 0 6 7 9 8 2 1 4 8 0 8 6 5 1 3 2

Note: This is a setting of the first one thousand decimal digits of Pi. Each single digit (0 - 9) is given the durational value of a semi quaver and each double digit (10, 11 etc.) is given the value of a quaver.

Note: There are a lot of repetitions in this infinite number, so repeated integers are given the combined duration of the repetitions (e.g. 9, 9, 9 would last for a dotted-quaver [three semi-quavers] and 8, 8, 8 would last for a crotchet [four semi-quavers].

Note: Whenever 1, 0 or 1, 1 appear in the cycle, they are treated as a 10 (B♭) and (B♯). Without this anomaly, 10 and 11 would never appear and this would therefore be a 10-tone row instead of a 12-tone row. This is referred to as 'the 10/11 anomaly.'

♩ = 108

[4 8 1 11]

[8 5 2 1 10]

8 2 3 0 6\* 4 7 0 9 3 8 4\* 6 0 9 5\* 0 5 8 2\* 3 1 7 2 5 3 5 9 4 0 8 1 2 8 4 8 11 1 7 4 5 0 2 8 4 10 2 7 0 1 9 3 8 5 2 11 0 5\*\* 9 6 4\* 6 2\* 9 4 8 9 5 4 9 3 0 3 8 1 9 6 4\* 2 8\* 10 9 7 5 6\* 5 9 3\* 4\* 6 1 2 8 4 7

15 5 6 4 8 2 3\* 7 8 6 7 8 3 1 6 5 2 7 1 2 0 1 9 0 9 1 4 5 6 4 8 5 6\* 9 2 3 4 6 0 3 4 8 6 10 4 5 4 3 2 6\* 4 8 2 1 3\* 9 3 6 0 7 2 6 0 2 4 9 1 4 1 2 7 3 7 2 4 5 8 7 0\* 6\* 0 6 3 1 5\* 8\* 1 7 4 8\* 1 5 2 0 9 2 0 9 6 2 8 2 9

poco rit.

[ $\downarrow = 104$ ]

poco accel..

J = 108

**B** ... a beginning of the end ...

5 4 9 5 8 5 3 7 10 5 0 7 9 2\* 7 9 6 8 9 2 5 8 9 2 3 5 4 2 0 1 9\* 5 6 11 2 1 2 9 0 2 1 9 6 0 8 6 4 0 3 4\* 1 8 1 5 9 8 1 3 6 2 9 7\* 4 7\* 1 3 0 9\* 6 0 5 1 8 7 0 7 2 11 3 4 9\*\*\*\*\* 8 3 7 2 9 7 8 0 4 9\* 5 10 5 9 7

43

3 1 7 3 2 8 1 6 0 9 6 3 1 8 5 9 5 0 2 4\* 5 9 4 5\* 3 4 6 9 0 8 3 0 2 6 4 2 5 2\* 3 0 8 2 5 3\* 4\* 6 8 5 0 3 5 2 6 1 9 3 11 8\* 1 7 10 10 0\* 3 1 3 7 8 3 8 7 5 2 8\* 6 5 8 7 5 3\* 2 0 8 3 8 1 4 2 0 6 1 7 1 7\* 6\* 9 1 4

50

poco rit. [♩ = 72] [6\* 1 11]

7 3 0 3 5 9 8 2 5 3 4 9 0 4 2 8 7 5\* 4 6 8 7 3 11 5 9 5 6 2 8 6 3 8\* 2 3 5 3 7 8 7 5 9 3 7 5 1 9 5 7\* 8 1 8 5 7\* 8 0 5 3 2 1 7 1 2\* 6 8 0 6\* 1 3 0\* 1 9 2 7 8 7 6\* 11 1 9 5 9 0 9 2 1 6 4 2 0 1 9 8

57

Note: In Cycle 2 there will never be a no.1 (unless it is affected by the 10/11 anomaly), as it will always be part of a double-digit. The amount of no.2s will also be reduced by 30%.

This does not negate the influence of the note C# (no.1), as it is statistically just as likely to appear as the number 13 as any other double-digit number. However, this starts to dilute the amount of notes in the very lowest register of the span, making the results sound more musical and also evolves naturally within the system.

Note: The barline cancels all accidentals and any accidentals refer only to that specific register.

### Cycle Two (a second of seven): Two octaves in 24 notes ...

**C**  $\text{♩} = 112$  Cycle 2: Two octave span (0 - 23) C4 - B5 [transposable up maximum of 2 octaves or down a maximum of 3 octaves and a minor third]: No reiterations (suspensions marked with an asterisk) ...

[8 2 14 8]

14 15 9 2 6 5 3 5 8 9 7 9 3 23 8 4 6 2 6 4 3\* 8 3 2 7 9 5 0 2 8\* 4 19 7 16 9 3 9\* 3 7 5 10 5 8 20 9 7 4 9 4\* 5 9 23 0 7 8 16 4 0 6 2 8 6 20 8 9\* 8 6 2 8 0 3 4 8 2 5 3 4 2 11 7 0 6 7 9 8 21 4 8 0 8 6 5 13 2

poco rit..

[♩ = 108]

[0 5 8 2 23 17 2]

[8 5 2 1 10]

8 23 0 6\* 4 7 0 9 3 8 4\* 6 0 9 5\* 0 5 8 22 3 17 2 5 3 5 9 4 0 8 12 8 4 8 11 17 4 5 0 2 8 4 10 2 7 0 19 3 8 5 2 11 0 5\*\* 9 6 4\* 6 22 9 4 8 9 5 4 9 3 0 3 8 19 6 4\* 2 8\* 10 9 7 5 6\* 5 9 3\* 4\* 6 12 8 4 7

poco accel..

[♩ = 112]

[2 7 1 20]

5 6 4 8 23 3 7 8 6 7 8 3 16 5 2 7 12 0 19 0 9 14 5 6 4 8 5 6\* 9 23 4 6 0 3 4 8 6 10 4 5 4 3 2 6\* 4 8 21 3\* 9 3 6 0 7 2 6 0 2 4 9 14 12 7 3 7 2 4 5 8 7 0\* 6\* 0 6 3 15 5 8\* 17 4 8\* 15 20 9 20 9 6 2 8 2 9

2 5 4 0 9 17 15 3 6 4 3 6 7 8 9 2 5 9 0 3 6 0\* 11 3\* 0 5 3 0 5 4 8\* 20 4 6\* 5 21 3 8 4 14 6 9 5 19 4 15 11 6 0 9 4 3\* 0 5 7 2 7 0 3 6 5 7 5 9 5 9 19 5 3 0 9 21 8 6 11 7 3 8 19 3 2 6 11 7 9 3 10 5 11 8 5

[2 13] [0 9 2 18]

mf mp

85

4 8 0 7 4\* 6 23 7 9\* 6 2 7 4 9 5 6 7 3 5 18 8 5 7 5 2 7 2 4 8 9 12 2 7 9 3 8 18 3 0 11 9 4 9 12 9 8 3\* 6 7 3\* 6 2 4\* 0 6 5 6\* 4 3 0 8 6 0 21 3 9 4 9 4 6 3 9 5 22 4 7 3 7 19 0 7 0 21 7 9 8 6 0 9 4 3 7 0 2 7\*

[8 9 1 22] [8 6 0 2 13] [2 17 9 8]

92

f mf

poco rit. [♩ = 108] poco accel. [♩ = 112]

[2 17 17] [2 14]

0 5 3 9 21 7 17 6 2 9 3 17 6 7 5 23 8 4 6 7 4 8 18 4 6 7 6\* 9 4 0 5 13 20 0\* 5 6 8 12 7 14 5 2 6 3 5 6 0 8 2 7\* 8 5 7\* 13 4 2 7 5 7\* 8 9 6 0 9 17 3 6 3 7 17 8 7 21 4 6 8 4\* 0 9 0 12 2 4 9 5 3 4 3 0 14 6

99

mp p mf mp

99

D ... a beginning of the end ...

[2 12 9 0 2 19 6 0]

5 4 9 5 8 5 3 7 10 5 0 7 9 22 7 9 6 8 9 2 5 8 9 23 5 4 20 19 9 5 6 11 21 2 9 0 21 9 6 0 8 6 4 0 3 4\* 18 15 9 8 13 6 2 9 7\* 4 7\* 13 0 9\* 6 0 5 18 7 0 7 2 11 3 4 9\*\*\*\*\* 8 3 7 2 9 7 8 0 4 9\* 5 10 5 9 7

106

*poco accel.* [♩ = 112] *poco rit.* [♩ = 108]

**[4 2 5 2 23 0 8 2 5]**

*ff* *mf* *f* *mf*

3 17 3 2 8 16 0 9 6 3 18 5 9 5 0 2 4\* 5 9 4 5\* 3 4 6 9 0 8 3 0 2 6 4 2 5 22 3 0 8 2 5 3\* 4\* 6 8 5 0 3 5 2 6 19 3 11 8\* 17 10 10 0\* 3 13 7 8 3 8 7 5 2 8\* 6 5 8 7 5 3\* 20 8 3 8 14 20 6 17 17 7 6\* 9 14

113

*ff* *mf*

*f* *mf*

*poco rit.* [♩ = 72]

[2 17 1 22]

7 3 0 3 5 9 8 2 5 3 4 9 0 4 2 8 7 5\* 4 6 8 7 3 11 5 9 5 6 2 8 6 3 8\* 23 5 3 7 8 7 5 9 3 7 5 19 5 7\* 8 18 5 7\* 8 0 5 3 21 7 12 2 6 8 0 6\* 13 0\* 19 2 7 8 7 6\* 11 19 5 9 0 9 21 6 4 20 19 8

*mp*

*p* *pp*

Note: In Cycle 3 there will never be a no.1 or 2 (unless they are affected by the 10/11 anomaly), as they will always be part of a double-digit. The amount of no.3s will also be reduced by 50%.  
 This dilutes the amount of notes in the very lowest register of the span, making the results sound more balanced in terms of timbre and also evolves naturally within the system as the span increases.

7

Note: The barline cancels all accidentals and any accidentals only refer to that specific register. Whenever there is a cross-stave beamed note, no rests are written in either stave.

### Cycle Three (a third of seven): Three octaves, but what register ...

E ♩ = 116 Cycle 3: Three octave span (0 - 35) C3 - B5 [transposable up maximum of two octaves, or down a maximum of two octaves and a minor third]: No Reiterations (suspensions marked with an asterisk) ...

14 15 9 26 5 35 8 9 7 9 32 3 8 4 6 26 4 33 8 32 7 9 5 0 28 8 4 19 7 16 9 3 9\* 3 7 5 10 5 8 20 9 7 4 9 4\* 5 9 23 0 7 8 16 4 0 6 28 6 20 8 9\* 8 6 28 0 34 8 25 34 2 11 7 0 6 7 9 8 21 4 8 0 8 6 5 13 28

[8 5 21 10]

23 0 6\* 4 7 0 9 3 8 4\* 6 0 9 5\* 0 5 8 22 31 7 25 35 9 4 0 8 12 8 4 8 11 17 4 5 0 28 4 10 27 0 19 3 8 5 2 11 0 5\*\* 9 6 4\* 6 22 9 4 8 9 5 4 9 30 3 8 19 6 4\* 28 8 10 9 7 5 6\* 5 9 33 4\* 6 12 8 4 7

5 6 4 8 23 3 7 8 6 7 8 31 6 5 27 12 0 19 0 9 14 5 6 4 8 5 6\* 9 23 4 6 0 34 8 6 10 4 5 4 32 6\* 4 8 21 33 9 3 6 0 7 26 0 24 9 14 12 7 3 7 24 5 8 7 0\* 6\* 0 6 31 5\* 8\* 17 4 8\* 15 20 9 20 9 6 28 29

25 4 0 9 17 15 3 6 4 3 6 7 8 9 25 9 0 3 6 0\* 11 33 0 5 30 5 4 8\* 20 4 6\* 5 21 3 8 4 14 6 9 5 19 4 15 11 6 0 9 4 33 0 5 7 27 0 3 6 5 7 5 9 5 9 19 5 30 9 21 8 6 11 7 3 8 19 32 6 11 7 9 3 10 5 11 8 5

148

4 8 0 7 4\* 6 23 7 9\* 6 27 4 9 5 6 7 35 18 8 5 7 5 27 24 8 9 12 27 9 3 8 18 30 11 9 4 9 12 9 8 33 6 7 33 6 24 4 0 6 5 6\* 4 30 8 6 0 21 3 9 4 9 4 6 3 9 5 22 4 7 3 7 19 0 7 0 21 7 9 8 6 0 9 4 3 7 0 27 7

155

poco rit.

[♩ = 112]

poco accel.

[♩ = 116]

0 5 3 9 21 7 17 6 29 31 7 6 7 5 23 8 4 6 7 4 8 18 4 6 7 6\* 9 4 0 5 13 20 0\* 5 6 8 12 7 14 5 26 35 6 0 8 27 7 8 5 7\* 13 4 27 5 7\* 8 9 6 0 9 17 3 6 3 7 17 8 7 21 4 6 8 4\* 0 9 0 12 24 9 5 34 30 14 6

162

**F** ... a beginning of the end ...

5 4 9 5 8 5 3 7 10 5 0 7 9 22 7 9 6 8 9 25 8 9 23 5 4 20 19 9 5 6 11 21 29 0 21 9 6 0 8 6 4 0 34 4 18 15 9 8 13 6 29 7\* 4 7\* 13 0 9\* 6 0 5 18 7 0 7 2 11 34 9\*\*\*\*\* 8 3 7 29 7 8 0 4 9\* 5 10 5 9 7

169

31 7 32 8 16 0 9 6 31 8 5 9 5 0 24 4 5 9 4 5\* 34 6 9 0 8 30 26 4 25 22 30 8 25 33 4\* 6 8 5 0 35 26 19 3 11 8\* 17 10 10 0\* 31 3 7 8 3 8 7 5 28 8 6 5 8 7 5 33 20 8 3 8 14 20 6 17 17 7 6\* 9 14

176

poco rit.

[♩ = 72]

7 30 35 9 8 25 34 9 0 4 28 7 5\* 4 6 8 7 3 11 5 9 5 6 28 6 3 8\* 23 5 3 7 8 7 5 19 5 7\* 8 18 5 7\* 8 0 5 32 17 12 26 8 0 6\* 13 0\* 19 27 8 7 6\* 11 19 5 9 0 9 21 6 4 20 19 8

183

Note: In Cycle 4 there will never be a no.1, 2 or 3 (unless they are affected by the 10/11 anomaly), as they will always be part of a double-digit. The amount of no.3s will also be reduced by 70%. This dilutes the amount of notes in the very lowest register of the span, making the results sound more balanced in terms of timbre and also evolves naturally within the system as the span increases.

Note: The barline cancels all accidentals and any accidentals only refer to that specific register. Whenever there is a cross-staff beamed note, no rests are written in either stave.

### Cycle Four (a fourth of seven): Let's just 'go for it' ...

**G** ♩ = 120 Cycle 4: Four octave span (0 - 47) C2 - B5 [transposable up maximum of two octaves, or down maximum of two octaves and a minor third]: No reiterations (suspensions are marked with an asterisk) ...

14 15 9 26 5 35 8 9 7 9 32 38 46 26 43 38 32 7 9 5 0 28 8 41 9 7 16 9 39 9 37 5 10 5 8 20 9 7 4 9 44 5 9 23 0 7 8 16 40 6 28 6 20 8 9\* 8 6 28 0 34 8 25 34 2 11 7 0 6 7 9 8 21 4 8 0 8 6 5 13 28

23 0 6\* 47 0 9 38 44 6 0 9 5\* 0 5 8 22 31 7 25 35 9 40 8 12 8 4 8 11 17 45 0 28 4 10 27 0 19 38 5 2 11 0 5\*\* 9 6 44 6 22 9 4 8 9 5 4 9 30 38 19 6 44 28 8 10 9 7 5 6\* 5 9 33 44 6 12 8 47

5 6 4 8 23 37 8 6 7 8 31 6 5 27 12 0 19 0 9 14 5 6 4 8 5 6\* 9 23 46 0 34 8 6 10 45 43 26 6 4 8 21 33 9 36 0 7 26 0 24 9 14 12 7 37 24 5 8 7 0\* 6\* 0 6 31 5\* 8\* 17 4 8\* 15 20 9 20 9 6 28 29

25 40 9 17 15 36 43 6 7 8 9 25 9 0 36 0\* 11 33 0 5 30 5 4 8\* 20 46 6 5 21 38 41 46 9 5 19 41 5 11 6 0 9 43 30 5 7 27 0 36 5 7 5 9 5 9 19 5 30 9 21 8 6 11 7 38 19 32 6 11 7 9 3 10 5 11 8 5

211

4 8 0 7 44 6 23 7 9\* 6 27 4 9 5 6 7 35 18 8 5 7 5 27 24 8 9 12 27 9 38 18 30 11 9 4 9 12 9 8 33 6 7 33 6 24 40 6 5 6\* 43 0 8 6 0 21 39 4 9 46 39 5 22 47 37 19 0 7 0 21 7 9 8 6 0 9 43 7 0 27 7

218

poco rit.

[♩ = 116]

poco accel.

[♩ = 120]

0 5 39 21 7 17 6 29 31 7 6 7 5 23 8 46 7 4 8 18 46 7 6\* 9 40 5 13 20 0\* 5 6 8 12 7 14 5 26 35 6 0 8 27 7 8 5 7\* 13 42 7 5 7\* 8 9 6 0 9 17 36 37 17 8 7 21 46 8 44 0 9 0 12 24 9 5 34 30 14 6

225

**H** ... a beginning of the end ...

5 4 9 5 8 5 37 10 5 0 7 9 22 7 9 6 8 9 25 8 9 23 5 42 0 19 9 5 6 11 21 29 0 21 9 6 0 8 6 40 34 41 8 15 9 8 13 6 29 7\* 47 7 13 0 9\* 6 0 5 18 7 0 7 2 11 34 9\*\*\*\*\* 8 37 29 7 8 0 4 9\* 5 10 5 9 7

232

31 7 32 8 16 0 9 6 31 8 5 9 5 0 24 45 9 45 5 34 6 9 0 8 30 26 42 5 22 30 8 25 33 44 6 8 5 0 35 26 19 3 11 8\* 17 10 10 0\* 31 37 8 38 7 5 28 8 6 5 8 7 5 33 20 8 38 14 20 6 17 17 7 6\* 9 14

239

poco rit.

[♩ = 72]

7 30 35 9 8 25 34 9 0 42 8 7 5\* 46 8 7 3 11 5 9 5 6 28 6 38 8 23 5 37 8 7 5 9 37 5 19 5 7\* 8 18 5 7\* 8 0 5 32 17 12 26 8 0 6\* 13 0\* 19 27 8 7 6\* 11 19 5 9 0 21 6 42 0 19 8

246

Note: In Cycle 5 there will never be a no.1, 2, 3 or 4 (unless they are affected by the 10/11 anomaly), as they will always be part of a double-digit. The amount of no.5s will also be radically reduced by 90%.  
This dilutes the amount of notes in the very lowest register of the span, making the results sound more balanced in terms of timbre and also evolves naturally within the system as the span increases.

13

Note: The barline cancels all accidentals and any accidentals only refer to that specific register. Whenever there is a cross-staff beamed note, no rests are written in either stave.

### Cycle Five (a fifth of seven): The hills are growing steeper ...

I  $\text{♩} = 120$  Cycle 5: Five octave span (0 - 59) C2 - B6 [transposable up maximum of one octave, or down a maximum of a compound minor third]: No reiterations (suspensions are marked with an asterisk) ...

14 15 9 26 53 58 9 7 9 32 38 46 26 43 38 32 7 9 50 28 8 41 9 7 16 9 39 9 37 5 10 58 20 9 7 49 44 59 23 0 7 8 16 40 6 28 6 20 8 9\* 8 6 28 0 34 8 25 34 2 11 7 0 6 7 9 8 21 48 0 8 6 51 32

253

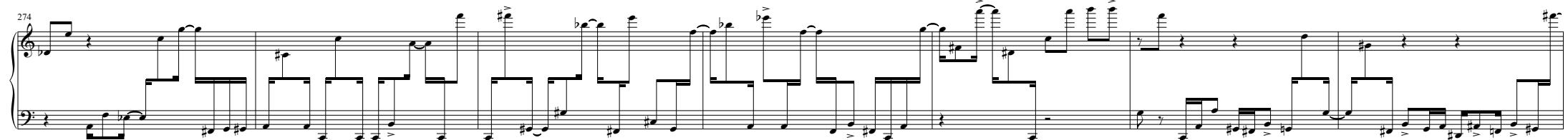
8 23 0 6\* 47 0 9 38 44 6 0 9 55 0 58 22 31 7 25 35 9 40 8 12 8 48 11 17 45 0 28 4 10 27 0 19 38 52 11 0 55 59 6 44 6 22 9 48 9 54 9 30 38 19 6 44 28 8 10 9 7 56 6 59 33 44 6 12 8 47

260

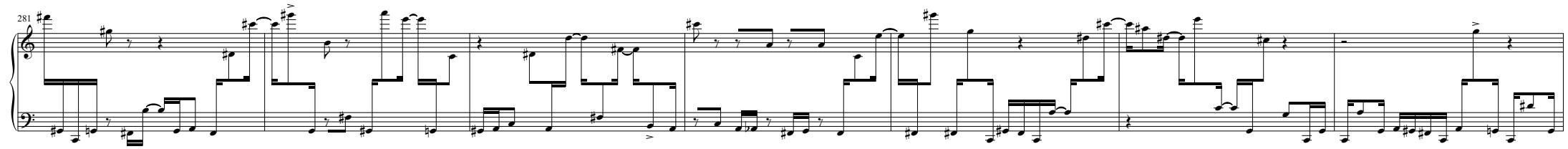
56 48 23 37 8 6 7 8 31 6 52 7 12 0 19 0 9 14 56 48 56 6 9 23 46 0 34 8 6 10 45 43 26 6 48 21 33 9 36 0 7 26 0 24 9 14 12 7 37 24 58 7 0\* 6\* 0 6 31 55 8\* 17 48 8 15 20 9 20 9 6 28 29

267

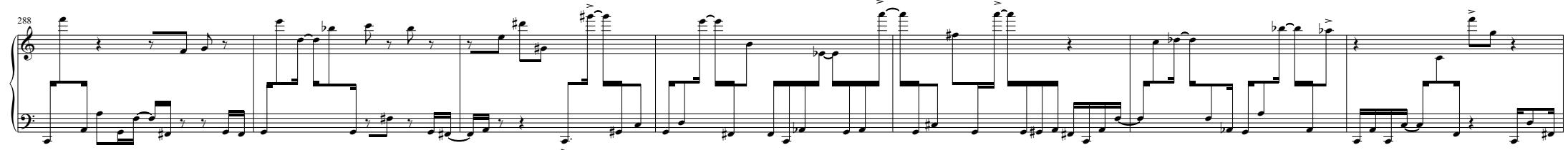
25 40 9 17 15 36 43 6 7 8 9 25 9 0 36 0 0 11 33 0 53 0 54 8\* 20 46 6 52 13 8 41 46 9 51 9 41 5 11 6 0 9 43 30 57 27 0 36 57 59 19 53 0 9 21 8 6 11 7 38 19 32 6 11 7 9 3 10 5 11 8 54



8 0 7 44 6 23 7 9\* 6 27 49 56 7 35 18 8 57 52 7 24 8 9 12 27 9 38 18 30 11 9 49 12 9 8 33 6 7 33 6 24 40 6 56 6 43 0 8 6 0 21 39 49 46 39 52 24 7 37 19 0 7 0 21 7 9 8 6 0 9 43 7 0 27 7



0 53 9 21 7 17 6 29 31 7 6 7 52 38 46 7 48 18 46 7 6\* 9 40 51 32 0\* 56 8 12 7 14 52 6 35 6 0 8 27 7 8 57 713 42 7 57 7 8 9 6 0 9 17 36 37 17 8 7 21 46 8 44 0 9 0 12 24 9 53 43 0 14 6



J ... a beginning of the end ...

54 9 58 53 7 10 50 7 9 22 7 9 6 8 9 25 8 9 23 54 20 19 9 56 11 21 29 0 21 9 6 0 8 6 40 34 41 8 15 9 8 13 6 29 7\* 47 7 13 0 9\* 6 0 51 8 7 0 7 2 11 34 9 9\* 9 9\* 8 37 29 7 8 0 49 9 5 10 59 7

31 7 32 8 16 0 9 6 31 8 59 50 24 45 9 45 53 46 9 0 8 30 26 42 52 23 0 8 25 33 44 6 8 50 35 26 19 3 11 8\* 17 10 10 0\* 31 37 8 38 7 52 8\* 6 58 7 53 32 0 8 38 14 20 6 17 17 7 6\* 9 14

poco rit. [♩ = 72]

7 30 35 9 8 25 34 9 0 42 8 7 55 46 8 7 3 11 59 56 28 6 38 8 23 53 7 8 7 59 9 37 51 9 57 7 8 18 57 7 8 0 53 21 7 12 26 8 0 6\* 13 0\* 19 27 8 7 6\* 11 19 59 0 9 21 6 42 0 19 8

Note: In Cycle 6 there will never be a no.1, 2, 3, 4, 5 or 6 (unless they are affected by the 10/11 anomaly), as they will always be part of a double-digit. The amount of no.7s will also be reduced by 10%. This dilutes the amount of notes in the very lowest register of the span, making the results sound more balanced in terms of timbre and also evolves naturally within the system as the span increases.

Note: The barline cancels all accidentals and any accidentals only refer to that specific register. Whenever there is a cross-staff beamed note, no rests are written in either stave.

### Cycle Six (a sixth of seven): Wake up, there are mountains to climb and things we can believe in ...

**K**  $\text{J} = 126$  Cycle 6: Six octave (0 - 71) C1 - B6 [transposable up a maximum of an octave or down a minor third]: No reiterations (suspensions are marked with an asterisk) ...

14 15 9 26 53 58 9 7 9 32 38 46 26 43 38 32 7 9 50 28 8 41 9 71 69 39 9 37 51 0 58 20 9 7 49 44 59 23 0 7 8 16 40 62 8 62 0 8 9\* 8 62 8 0 34 8 25 34 21 17 0 67 9 8 21 48 0 8 65 13 28

316

mp

mf

mp

mf

mp

23 0 66 47 0 9 38 44 60 9 55 0 58 22 31 7 25 35 9 40 8 12 8 48 11 17 45 0 28 41 0 27 0 19 38 52 11 0 55 59 64 46 22 9 48 9 54 9 30 38 19 64 42 8\* 10 9 7 56 65 9 33 44 61 28 47

323

mf

mp

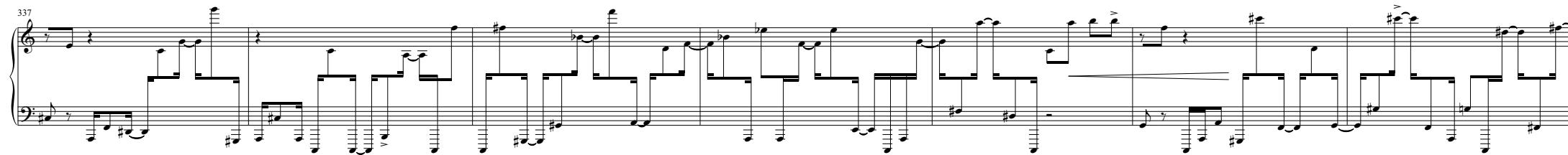
56 48 23 37 8 67 8 31 65 27 12 0 19 0 9 14 56 48 56 69 23 46 0 34 8 61 0 45 43 26 64 8 21 33 9 36 0 7 26 0 24 9 14 12 7 37 24 58 7 0\* 66 0 63 15 58 8 17 48 8 15 20 9 20 9 62 8 29

330

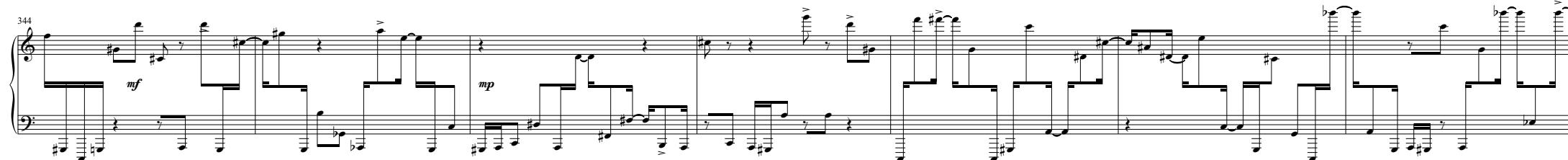
mf

mp

25 40 9 17 15 36 43 67 8 9 25 9 0 36 0\* 11 33 0 53 0 54 8\* 20 46 65 21 38 41 46 9 51 9 41 51 16 0 9 43 30 57 27 0 36 57 59 59 19 53 0 9 21 8 61 17 38 19 32 61 17 9 31 0 51 18 54



8 0 7 44 62 37 9\* 62 7 49 56 7 35 18 8 57 52 7 24 8 9 12 27 9 38 18 30 11 9 49 12 9 8 33 67 33 62 44 0 65 66 43 0 8 60 21 39 49 46 39 52 24 7 37 19 0 70 21 7 9 8 60 9 43 70 27 70



53 9 21 71 7 62 9 31 7 67 52 38 46 7 48 18 46 7 66 9 40 51 32 0\*\* 56 8 12 71 45 26 35 60 8 27 7 8 57 71 34 27 57 7 8 9 60 9 17 36 37 17 8 7 21 46 8 44 0 9 0 12 24 9 53 43 0 14 65



**L** ... a beginning of the end ...

49 58 53 71 0 50 7 9 22 7 9 68 9 25 8 9 23 54 20 19 9 56 11 21 29 0 21 9 60 8 64 0 34 41 8 15 9 8 13 62 9 7\* 47 71 30 9\* 60 51 8 70 7 21 13 49 9 9\* 9\* 8 37 29 7 8 0 49 9 51 0 59 7

31 7 32 8 16 0 9 63 18 59 50 24 45 9 45 53 46 9 0 8 30 26 42 52 23 0 8 25 33 44 68 50 35 26 19 31 18 8 17 10 10 0\* 31 37 8 38 7 52 8\* 65 8 7 53 32 0 8 38 14 20 61 71 7\* 66 9 14

poco rit.

[♩ = 72]

7 30 35 9 8 25 34 9 0 42 8 7 55 46 8 7 31 15 9 56 28 63 8\* 23 53 7 8 7 59 37 51 9 57 7 8 18 57 7 8 0 53 21 71 22 68 0 66 13 0\* 19 27 8 7 66 11 19 59 0 9 21 64 20 19 8

Note: In Cycle 7 there will never be a no.1, 2, 3, 4, 5, 6 or 7 (unless they are affected by the 10/11 anomaly), as they will always be part of a double-digit. The amount of no.8s will also be reduced by 30%. This dilutes the amount of notes in the very lowest register of the span, making the results sound more balanced in terms of timbre and also evolves naturally within the system as the span increases.

19

Note: The barline cancels all accidentals and any accidentals only refer to that specific register. Whenever there is a cross-staff beamed note, no rests are written in either stave.

### Cycle Seven (the seventh of seven): In leaps and bounds - a mission impossible ...

**M** ♪ = 132 Cycle 7: Seven octave (0 - 83) C1 - B7 (only transposable down a minor third): No reiterations (suspensions are marked with an asterisk \*) ...

14 15 9 26 53 58 9 79 32 38 46 26 43 38 32 79 50 28 8 41 9 71 69 39 9 37 51 0 58 20 9 74 9 44 59 23 0 78 16 40 62 8 62 0 8 9\* 8 62 80 34 82 53 42 11 70 67 9 82 14 80 8 65 13 28

379

mp

23 0 66 47 0 9 38 44 60 9 55 0 58 22 31 72 53 59 40 81 28 48 11 17 45 0 28 41 0 27 0 19 38 52 11 0 55 59 64 46 22 9 48 9 54 9 30 38 19 64 42 8 81 0 9 75 66 59 33 44 61 28 47

[Note: E major]

386

mp

56 48 23 37 8 67 83 16 52 71 20 19 0 9 14 56 48 56 69 23 46 0 34 8 61 0 45 43 26 64 82 13 39 36 0 72 60 24 9 14 12 73 72 45 8 70 0 66 0 63 15 58 81 74 8 81 52 0 9 20 9 62 82 9

393

25 40 9 17 15 36 43 67 8 9 25 9 0 36 0\* 11 33 0 53 0 54 8 82 0 46 65 21 38 41 46 9 51 9 41 51 16 0 9 43 30 57 27 0 36 57 59 59 19 53 0 9 21 8 61 17 38 19 32 61 17 9 31 0 51 18 54

80 74 46 23 79 9 62 74 9 56 73 51 8\* 57 52 72 48 9 12 27 9 38 18 30 11 9 49 12 9 83 36 73 36 24 40 65 66 43 0 8 60 21 39 49 46 39 52 24 73 71 9 0 70 21 79 8 60 9 43 70 27 70

53 9 21 71 76 29 31 76 75 23 8 46 74 81 8 46 76 69 40 51 32 0\*\* 56 81 27 14 52 63 56 0 82 77 8 57 71 34 27 57 78 9 60 9 17 36 37 17 8 72 14 68 44 0 9 0 12 24 9 53 43 0 14 65

The image shows three staves of piano sheet music. The top staff begins at measure 400, featuring a treble clef, a key signature of one sharp, and a common time signature. It contains a series of eighth-note patterns with various dynamic markings like crescendos and decrescendos. The middle staff begins at measure 407, also in treble clef and common time, with a different set of eighth-note patterns and dynamics. The bottom staff begins at measure 414, in treble clef and common time, with yet another set of eighth-note patterns and dynamics. Each staff includes a list of numerical values above the staff, likely representing specific notes or performance parameters.

**N** ... the beginning of the end ...

This image shows a page of sheet music for piano, page 10, containing measures 49 through 73. The music is in common time and includes two staves: treble and bass. The treble staff features a series of eighth-note patterns with various dynamics like forte (f), piano (p), and mezzo-forte (mf). The bass staff provides harmonic support with sustained notes and rhythmic patterns. Measure numbers are listed above the staff, and measure 421 is indicated at the beginning of the section.

poco rit.

[• = 76]

# **An Infinite Circle is a Straight Line**

... a thousand sounds of pi ...

For solo piano

Analysis Score: Cycles 1 – 7

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2012/20

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